Comments on “Capacity of Byzantine Agreement”*

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Technical Report

January 29, 2010

In our previous work [1] we proposed an algorithm to achieve Byzantine agreement in a four node network at rate of $R$ given that a set of link capacity constraints are satisfied (Inequalities 2 to 16 in [1]). Recently, we discovered that only inequalities 2 to 13 are necessary. Moreover, we also found that they are also sufficient if the inequalities are strict. We are able to prove the sufficiency of the strict inequalities by construction. In particular, we introduced an agreement algorithm that achieves agreement throughput arbitrarily close to $R$.

1 Capacity of the Four Node Network

Consider the same four node network in [1]. Figure 1 shows the four-node network. The labels near the various links denote the link capacities. Without loss of generality, we assume that $k \leq l \leq m$.

The the following constraints are necessary for agreement throughput of $R$ to be achievable:

- If one of the peers is removed from the network, then these conditions must be true for the min-cut from $S$ to a remaining peer to be at least $R$:

$$k + l \geq R$$  \hspace{1cm} (1)

*This research was supported in part by Army Research Office grant W-911-NF-0710287
The max-flow to one of the peers from the other two peers, with sender S removed, must be at least $R$.

- $p + q \geq R$  
- $r + s \geq R$  
- $t + u \geq R$

Without loss of generality, we assume that $k \leq l \leq m$.

- $l + m \geq R$  
- $m + k \geq R$  
- $p + k \geq R$  
- $q + k \geq R$  
- $r + l \geq R$  
- $s + l \geq R$  
- $t + m \geq R$  
- $u + m \geq R$
The necessity of the above conditions are already shown in [1]. The proof of sufficiency when the inequalities are strict will be released later this year.

References

