On Staggered Checkpointing

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Abstract

A consistent checkpointing algorithm saves a consistent view of a distributed application's state on stable storage. The traditional consistent checkpointing algorithms require different processes to save their state at about the same time. This causes contention for the stable storage, potentially resulting in large overheads. Staggering the checkpoints taken by various processes can reduce checkpoint overhead [10]. This paper presents a simple approach to arbitrarily stagger the checkpoints. Our approach requires that the processes take consistent logical checkpoints, as compared to consistent physical checkpoints enforced by existing algorithms. Experimental results on nCube-2 are presented.

1 Introduction

Applications executed on a large number of processors, either in a distributed environment, or on multicomputers such as nCube, are subject to processor failures. Consistent checkpointing is a commonly used technique to prevent complete loss of computation upon a failure [1, 3, 5, 9, 10]. A consistent checkpointing algorithm saves a consistent view of a distributed application's state on a stable storage. The loss of computation upon a failure is bounded by taking consistent checkpoints with adequate frequency.

The traditional consistent checkpointing algorithms require different application processes to save their state at about the same time. This causes contention for the stable storage, potentially resulting in significant performance degradation [10]. Staggering the checkpoints taken by various processes can reduce the overhead of consistent checkpointing by reducing stable storage contention. Some techniques for staggering the checkpoints have been previously proposed [10], however, these techniques result in "limited" staggering in that not all processes' checkpoints can be staggered. Ideally, one would like to stagger the checkpoints arbitrarily. If processors are able to make an "in-memory" copy of entire process state, then checkpoint staggering is trivial. This paper considers systems where it is not feasible to make an in-memory copy of entire process state. This situation may occur because: (i) memory size is small, or (ii) the memory may be shared by processes of multiple applications — making in-memory copy of a process from one application may cause processes from other applications to be swapped out (degrading their performance).

This paper presents a simple approach to arbitrarily stagger the checkpoints. Our approach requires that the processes take consistent logical checkpoints, as compared to consistent physical checkpoints enforced by existing algorithms for staggering. The paper discusses the proposed approach and presents experimental results on nCube-2 multicomputer.

2 Related Work

Plank [10] was the first to observe that stable storage contention can be serious problem for consistent checkpointing, and suggested checkpoint staggering as a solution. The degree of staggering with Plank's algorithm (based on the Chandy-Lamport algorithm [1]) is completely dependent on the application's communication pattern. In contrast, our algorithm allows arbitrary staggering of the checkpoints, independent of the application. Plank [10] also presents another approach for staggering checkpoints, that is applicable to wormhole routed networks. This algorithm also does not permit arbitrary/controlled staggering.

Long et al. [9] discuss an evolutionary checkpoint-
A Logical Checkpoint

A process is said to be deterministic if its state depends only on its initial state and the messages delivered to it [5, 11]. A deterministic process can take two types of checkpoints: a physical checkpoint or a logical checkpoint. A process is said to have taken a physical checkpoint at some time \( t_1 \) if the process state at time \( t_1 \) is saved on the stable storage. A process is said to have taken a logical checkpoint at time \( t_1 \), if adequate information is saved on the stable storage to allow the process state at time \( t_1 \) to be recovered. A physical checkpoint is trivially a logical checkpoint, however, the converse is not true. Now we summarize three approaches for taking a logical checkpoint at time \( t_1 \). Each approach may be more attractive for some applications than the other approaches. Not all approaches will be feasible on all systems.

**Approach 1:** One approach for establishing a logical checkpoint at time \( t_1 \) is to take a physical checkpoint at some time \( t_0 \leq t_1 \) and log (on stable storage) all messages delivered to the process between time \( t_0 \) and \( t_1 \). (For each message, the message log contains the receive sequence number for the message as well as the entire message.) This approach is essentially identical to that presented by Wang et al. [13].

Figure 1 presents an example wherein process \( P \) takes a physical checkpoint at time \( t_0 \). Messages M1, M2 and M3 are delivered to process \( P \) by time \( t_1 \). To establish a logical checkpoint of process \( P \) at time \( t_1 \), messages M1, M2 and M3 are logged on the stable storage. As process \( P \) is deterministic, the state of process \( P \) at time \( t_1 \) can be recovered using the information on the stable storage (i.e., physical checkpoint at \( t_0 \) and messages M1, M2 and M3).

We summarize this approach as:

\[
\text{physical checkpoint} + \text{message log} = \text{logical checkpoint}
\]

**Approach 2:** The essential purpose behind saving the messages above is to be able to recreate the state at time \( t_1 \), or to be able to "re-perform" the incremental changes made in process state by each of these messages. This may be achieved simply by taking a physical checkpoint at time \( t_0 \) and taking an incremental checkpoint at time \( t_1 \). The incremental checkpoint is taken by logging the changes made to process state between time \( t_0 \) and \( t_1 \). We summarize this approach as:

\[
\text{physical checkpoint} + \text{incremental checkpoint} = \text{logical checkpoint}
\]

The evolutionary checkpointing scheme by Long et al. [9] takes checkpoints similar to above procedure, although they do not use the term logical checkpoint.

**Approach 3:** The above two approaches take a physical checkpoint prior to the desired logical checkpoint, followed by logging of additional information (either messages or incremental state change).

The third approach is the converse of the above two approaches. Here, the physical checkpoint is taken at a time \( t_2 \), where \( t_2 > t_1 \). In addition, enough information is saved to undo the effect of messages received between time \( t_1 \) and \( t_2 \). For each relevant message (whose effect must be undone), an anti-message is

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1The term logging is used to mean "saving on the stable storage".
Figure 2: Anti-message log + physical checkpoint = logical checkpoint

Figure 3: Recovering a logical checkpoint using anti-messages

saved on the stable storage. The notion of an anti-message here is similar to that used in time warp mechanism [4] or that of UNDO records [2] in database systems. Anti-message M* corresponding to a message M can be used to undo the state change caused by message M.

Figure 2 illustrates this approach. A logical checkpoint of process P is to be established at time t1. Process P delivers messages M4 and M5 between time t1 and t2. A physical checkpoint is taken at time t2, and anti-messages corresponding to messages M4 and M5 are logged on the stable storage. The anti-messages are named M4* and M5*, respectively.

To recover the state, say S1, of process P at time t1, the process is initialized to the physical checkpoint taken at time t2 and then anti-messages M5* and M4* are sent to the process. The order in which the anti-messages are delivered is reverse the order in which the messages were delivered. As shown in Figure 3, the final state of process P is identical to the state (or logical checkpoint) at time t1.

We summarize this approach as:

anti-message log + physical checkpoint = logical checkpoint

An important issue is that of forming the anti-messages. The anti-messages can possibly be formed by the application itself, or they may consist of a copy of the (old) process state modified by the message (similar to copy-on-write [8]).

4 Chandy-Lamport Algorithm [1]

Chandy and Lamport [1] presented an algorithm for taking a consistent checkpoint of a distributed system. Assume that the processes communicate with each other using unidirectional communication channels; a bidirectional channel can be modeled as two unidirectional channels. For simplicity, we assume that the communication graph is fully connected.3

The algorithm presented next is essentially identical to Chandy-Lamport [1, 10] and assumes that a certain process (named P0) is designated as the checkpoint coordinator.

Algorithm: The coordinator process P0 initiates the consistent checkpointing algorithm by sending marker messages on each channel, incident on, and directed away from P0 and immediately takes a checkpoint. (This is a physical checkpoint.)

A process, say Q, on receiving a marker message along a channel c takes the following steps:

if Q has not taken a checkpoint then
begin
Q sends a marker on each channel, incident on, and directed away from Q.
Q takes a checkpoint.
Q records the state of channel c as being empty.
end
else Q records the state of channel c as the sequence of messages received along c, after Q had taken a checkpoint and before Q received the marker along c.

4.1 Plank's Staggering Scheme [10]

Plank [10] suggested that the processes should send markers after taking their checkpoints, rather than before taking the checkpoint (unlike the algorithm above). This simple modification introduces some staggering of checkpoints. However, not all checkpoints can be staggered.

In our experiments, we use the Chandy-Lamport algorithm that incorporates Plank's modification. In the rest of this paper, this modified algorithm will be referred to as Chandy-Lamport/Plank algorithm, or CL/P for brevity.

Note that Chandy-Lamport algorithm is applicable to strongly connected graphs. Our algorithm can also be generalized to strongly connected graphs.
Observations: Plank [10] observed that his staggering schemes work better than the original “non-staggered” algorithm when (i) degree of synchronization amongst the processes is relatively small, and (ii) the message volume is relatively small.

5 Staggered Consistent Checkpointing

The extent of checkpoint staggering using CL/P algorithm is dependent on the application’s communication pattern, and also on how the algorithm is implemented (e.g., whether the markers are sent synchronously or asynchronously). On the other hand, the proposed algorithm can stagger the checkpoints in any manner desired. Many variations are possible, depending on which checkpoints are desired to be staggered [12]. As an illustration, we assume that the objective is to stagger all checkpoints, i.e., no two checkpoints should overlap in time. Later, we will illustrate a situation where some overlap in checkpointing is desired.

The proposed algorithm (named STAGGER) can be summarized as follows:

staggered physical checkpoints + consistent logical checkpoints = staggered consistent checkpoints

The basic idea is to coordinate logical checkpoints rather than physical checkpoints. In this section, we assume that the first approach, described in Section 3, for taking logical checkpoints is being used. Thus, a logical checkpoint is taken by logging all messages delivered to a process since its most recent physical checkpoint.

For the purpose of this discussion, assume that the checkpoint coordinator is named $P_0$, and other processes are named $P_1$ through $P_{n-1}$. ($n$ is the number of processes.)

We now present the proposed algorithm (consisting of two phases), followed by an illustration. Presently, we assume that all processors share a single stable storage; Section 7 considers the situation where multiple stable storages are available.

Algorithm STAGGER

1. Physical checkpointing phase: Checkpoint coordinator $P_0$ takes a physical checkpoint and then sends a `take_checkpoint` message to process $P_1$.

When a process $P_i$, $i > 0$, receives a `take_checkpoint` message, it takes a physical checkpoint and then sends a `take_checkpoint` message to process $P_j$, where $j = (i + 1) \mod n$.

When process $P_0$ receives a `take_checkpoint` message from process $P_{n-1}$, it initiates the second phase of the algorithm (named consistent logical checkpointing phase).

After a process takes the physical checkpoint, it continues execution. Each message delivered to the process, after taking the physical checkpoint (but before the completion of the next phase), is logged in the stable storage.

The above procedure ensures that physical checkpoints taken by the processes are staggered because only one process takes a physical checkpoint at any time. The physical checkpoints taken by the processes are not, in general, necessarily consistent. (No attempt is made to ensure consistency of physical checkpoints.)

2. Consistent logical checkpointing phase: This phase is very similar to the Chandy-Lamport algorithm. The difference between Chandy-Lamport algorithm and this phase is that when the original Chandy-Lamport algorithm requires a process to take a “checkpoint”, our processes take a logical checkpoint (not a physical checkpoint as in the Chandy-Lamport algorithm). A logical checkpoint is taken by ensuring that the messages delivered since the physical checkpoint (taken in the previous phase) are logged on stable storage. The exact algorithm for this phase is provided below:

Initiation: The coordinator $P_0$ initiates this phase on receipt of the `take_checkpoint` message from process $P_{n-1}$. Process $P_0$ sends marker message on each channel, incident on, and directed away from $P_0$. Also, $P_0$ takes a logical checkpoint by ensuring that all messages delivered to it since its physical checkpoint are logged.

A process, say $Q$, on receiving a marker message along a channel $c$ takes the following steps:

if $Q$ has not taken a logical checkpoint then
    begin
        $Q$ sends a marker on each channel, incident on, and directed away from $Q$.
        $Q$ takes a logical checkpoint by ensuring that all messages delivered to it (on any channel) after $Q$’s recent physical checkpoint have been logged.
    end
else $Q$ ensures that all messages received on channel $c$ since its recent logical checkpoint are logged.

Messages received on channel $c$ after a marker is received on that channel are not logged. Similar to
the Chandy-Lamport algorithm, messages sent by a process before its logical checkpoint, but not received before the receiver’s logical checkpoint are logged as part of the channel state. Note that a message M that is logged to establish a logical checkpoint may be logged any time from the instant it is received until the time when the logical checkpoint is to be established. In our implementation, due to insufficient memory on nCube-2, such messages were logged immediately on receipt.

The above algorithm establishes a consistent recovery line consisting of one logical checkpoint per process. This algorithm reduces the contention for the stable storage by completely staggering the physical checkpoints. However, contention is now introduced in the second phase of the algorithm when the processes log messages. Our scheme will perform well if message volume is relatively small compared to checkpoint sizes. As suggested by a referee, if markers are sent after logging message (in the second phase), then stable storage contention may potentially be smaller. A few other variations of the above algorithm are possible, as discussed in Section 7.

Figure 4 illustrates the algorithm assuming that the system consists of three processes. Process $P_0$ acts as the coordinator and initiates the checkpointing phase by taking a physical checkpoint and sending a take_checkpoint message to $P_1$. Processes $P_0$, $P_1$, and $P_2$ take staggered checkpoints during the first phase. When process $P_0$ receives take_checkpoint message from process $P_1$, it initiates the consistent logical checkpointing phase. Process $P_0$ sends marker messages to $P_1$ and $P_2$ and then takes a logical checkpoint by logging messages $M_0$ and $M_2$ on the stable storage. When process $P_1$ receives the marker message from process $P_0$, it sends markers to $P_0$ and $P_2$ and then takes a logical checkpoint by logging message $M_1$ on the stable storage. Similarly, process $P_2$ takes a logical checkpoint by logging message $M_3$ on the stable storage. Messages $M_4$ and $M_5$ are also logged during the second phase (as they represent the channel state).

**Recovery:** After a failure, each process rolls back to its recent physical checkpoint and re-executes (using the logged messages) to restore the process state to the logical checkpoint that belongs to the most recent consistent recovery line.

**Proof of correctness:** The correctness follows directly from the proof of correctness for the Chandy-Lamport algorithm [1].

### 6 Performance Evaluation

We implemented the proposed algorithm STAGGER and the Chandy-Lamport/Plank scheme (abbreviated as CL/P) on a nCube-2 multicomputer. It should be noted that performance of each scheme is closely dependent on the underlying hardware and behavior of the application program. Clearly, no single scheme can perform well on all applications. Our objective here is to demonstrate that the proposed algorithm can perform well under certain circumstances.

In our implementation of CL/P and STAGGER, the markers sent by node 0 are sent asynchronously using interrupts – sufficient care is taken to ensure that the markers appear in FIFO order with respect to other messages even though they are sent asynchronously. Markers sent by other processes are sent without using interrupts. If no markers are sent asynchronously, the checkpointing algorithm may not make progress in the cases where synchronization (or communication) is very infrequent. As staggering can be useful primarily under these circumstances, it is necessary to ensure that the algorithm progresses without any explicit communication by application processes. We will return to the issue of using asynchronous markers later in Section 7.

The application used for evaluation is a synthetic program, named sync-loop, similar to a program used by Plank [10]. The pseudo-code for the program is presented below.

```plaintext
csync-loop(iter, size, M) {
    state = malloc(size); // create state
    initialize (state);
```
repeat (iter) times {
    perform $M$ floating-point multiplications;
    synchronize with all other processes;
}
}

Process state size (and checkpoint size) is controlled by the size parameter. Each process repeats a loop in which it performs some computation (the amount of computation controlled by the $M$ parameter). The loop is repeated iter times.

By choosing a very large value for $M$ the degree of synchronization in the program is minimized. A small $M$, on the other hand, implies that processes synchronize very frequently. Synchronization is achieved by means of an all-to-all message exchange.

Figure 5 presents experimental results for STAGGER and CL/P schemes. Synchronization interval is the time between two consecutive synchronizations of the processes – thus, synchronization interval is approximately equal to the time required to perform the computation (i.e., the $M$ multiplications) in each iteration of the loop. The checkpoint size for each process is approximately 2.1 Mbyte. Checkpoint overhead is obtained as: (execution time with $S$ consistent checkpoints − execution time without any checkpoints)$/S$. For our measurements, $S = 5$ (that is, five checkpoints per execution of the program). Each instance of the application was executed five times, and checkpoint overhead was averaged over these five executions.

Figure 5 presents overhead measurements for experiments on a cube of dimension 1, 2, 3 and 4. Curve labeled $d = N$ in the figure is for experiments on $N$-dimensional cube. (Labels (a) through (h) can be used to match the curves with the corresponding labels in top right corner of the figure.) All processes shared a single disk to store the checkpoints. We choose to plot absolute values of checkpoint overhead, instead of percentage overhead, as absolute overhead is independent of the checkpoint interval, unlike percentage overhead. In Figure 5, observe that, for a fixed dimension, as the synchronization interval becomes smaller, the checkpoint overhead grows for both schemes. For very small synchronization intervals, the STAGGER scheme does not perform much better than the Chandy-Lamport/Plank scheme. However, when synchronization interval is large, the proposed scheme achieves significant improvements. (For dimension $d = 1$, the two schemes achieve essentially identical performance.)

Observe in Figure 5 that, for a given instance of the application, as the dimension is increased the overhead for STAGGER as well as CL/P increases. However, the increase in the overhead of CL/P is much greater than that of STAGGER.

The stable storage contention tends to increase with an increase in the number of application processes. To better understand the impact of stable storage contention, in Figure 6, we plot the ratio (checkpoint overhead/number of nodes). Observe that, for a given instance of the application, the ratio is higher for larger dimension when using the CL/P scheme – on the other hand, the ratio is smaller for larger dimension when using the STAGGER scheme. The reason being that the increase in the overhead of STAGGER, with increasing dimension, is relatively small as compared to CL/P.

The measurements presented above imply that when the parallel application has a large granularity (thus, requiring infrequent communication or synchronization), the proposed STAGGER algorithm can perform well. As an example of an application with coarse-grain parallelism we present measurements for a simulation program (SIM), in Figure 7. The simu-
checkpoint overhead (second) / number of nodes

synchronization interval (second)

(a) CL/P    d=4
(b) Stagger d=4
(c) CL/P    d=3
(d) Stagger d=3
(e) CL/P    d=2
(f) Stagger d=2
(g) CL/P    d=1
(h) Stagger d=1

Figure 6: (Checkpoint overhead/number of nodes) for sync-loop program

Figure 7: Measurements for SIM application

The simulation program evaluates the expected execution time of a task when using rollback recovery. State size for each process in SIM is approximately 34 Kbyte. The simulation program is completely parallelized, and the processes synchronize only at the beginning and at the completion of the simulation. This synchronization pattern represents the best possible scenario for staggered checkpointing. As seen from Figure 7, the checkpoint overhead for STAGGER remains constant independent of the dimension, as synchronization is very infrequent. On the other hand, the overhead for CL/P increases with the dimension.

Impact of message size on performance: Plank [10] observed that his staggered checkpointing schemes log more messages than non-staggered checkpointing schemes. Therefore, his schemes do not perform well compared to non-staggering schemes, when message sizes are large. Similarly, as the STAGGER algorithm staggers checkpoints more than Plank’s algorithm, it tends to log more messages than Plank’s algorithm. Therefore, STAGGER will not perform well when message sizes are large. This conclusion follows directly from that made previously by Plank.

7 Variations on the Theme

Many variations of the algorithm presented earlier are possible. Utility of these variations depends on the nature of the application and the execution environment. In the following, we discuss some variations.

(a) Process clustering to exploit multiple stable storages: The algorithm STAGGER presented above assumes that all processes share a single stable storage. However, in some systems, the processes may share multiple stable storages. For instance, number of processes may be 16 and the number of stable storages may be 4. For such systems, we modify the proposed STAGGER algorithm to make use of all stable storages while minimizing contention for each stable storage. To achieve this we partition the processes into clusters, the number of clusters being identical to the number of stable storages. Each cluster is associated with a unique stable storage; processes within a cluster access only the associated stable storage [7].

The algorithm STAGGER, modified to use multiple stable storages, differs from the original STAGGER algorithm only in the first phase (i.e., staggered checkpointing phase). We illustrate the modified staggered checkpointing phase with an example. Consider a system consisting of 6 processes, and 2 stable storages. The processes are now named $P_{ij}$, where $i$ denotes the cluster number and $j$ denotes the process number
within the cluster. As 2 stable storages are available, the processes are divided into 2 clusters containing 3 processes each. Cluster \( i \) \((i = 0,1)\) contains processes \( P_{i0}, P_{i1}, \text{and} P_{i2} \). Process \( P_{i0} \) in cluster \( i \) is identified as the checkpoint coordinator for cluster \( i \), and process \( P_{00} \) is also identified as the global checkpoint coordinator. Figure 8 depicts the first phase of the modified algorithm.

![Figure 8: Process clustering to utilize multiple stable storages](image)

(b) Approach for taking a logical checkpoint: The discussion so far assumed that a logical checkpoint is taken by taking a physical checkpoint and logging subsequently received messages. The proposed algorithm can be easily modified to allow a process to use any of the three approaches presented earlier (in Section 3) for establishing a logical checkpoint. In fact, different processes may simultaneously use different approaches for establishing a logical checkpoint.

(c) Checkpointing versus message logging: As staggering tends to increase the number of messages logged, the following variations will be beneficial for some applications.

- A process may decide to not take a physical checkpoint in the first phase, if it \( \text{a priori} \) knows that its message log will be large. In this case, the process would take a physical checkpoint in the second phase.\(^3\)

- If a process receives too many messages after taking the physical checkpoint in the first phase of the algorithm, then it may decide to take a physical checkpoint in the second phase (rather than logging messages). This makes the physical checkpoint taken by the process in the first phase redundant. However, this modification may reduce the overhead when checkpoint size is smaller than what the message log would be.

(d) A synchronous Markers:

An asynchronous marker is one which is detected by the destination process soon after it is received. Arrival of an asynchronous marker is informed to the destination process by means of an interrupt (or signal). In spite of the asynchronous nature, the marker appears in its appropriate position on the FIFO channel on which it is sent. We call a marker that is not sent with an interrupt a “synchronous” marker (for the lack of a better terminology). While an asynchronous marker can be processed as soon as it arrives, a synchronous marker may not be processed for a long time – particularly, if the destination process does not need any messages on the corresponding channel.

Which markers (if any) are sent asynchronously can affect performance of STAGGER and CL/P algorithms significantly. As noted previously, in our implementation, markers sent by process 0 are asynchronous, other markers are synchronous.

One variation on Plank's scheme [10] for applications with infrequent synchronization (communication) is as follows: Ensure that the marker sent by process \( i \) to process \( j \) is asynchronous if and only if \( j = i + 1 \) (modulo number of processes). Thus, each process will take checkpoint, and the algorithm

\(^3\)Johnson [8] suggested a scheme where each process uses a similar heuristic to decide whether to log messages or not.
will make progress, even if the processes are not communicating with each other. Also, as each process sends only one asynchronous marker, the algorithm would tend to reduce contention for the stable storage. With infrequent synchronization (communication) the above rule will completely stagger checkpoints by the different processes (i.e., the algorithm becomes similar to STAGGER).

(e) Initiation of Logical Checkpointing Phase: In our description of the STAGGER algorithm, we assume that only process 0 initiates the second phase (consistent logical checkpointing) of the algorithm. Note that the second phase of the algorithm is identical to the original Chandy-Lamport algorithm, with the exception that physical checkpoints are replaced by logical checkpoints. The Chandy-Lamport algorithm can be implemented correctly with multiple initiators also. Therefore, the STAGGER algorithm can be modified to allow any process to initiate the second phase at any time. Different heuristics for deciding who starts the second phase and when can yield different performance. One heuristic, similar to one mentioned earlier, is to allow a process to initiate the second phase immediately after taking physical checkpoint in the first phase, if it is known that the process will need to log too many large messages.

Clearly, there are many variations possible based on the STAGGER algorithm. Also, staggering is not always beneficial. (In general, no single checkpointing scheme works well for all possible applications.) A future goal of our research is to design an adaptive algorithm that can, at run-time, determine if staggering is beneficial or not (and which staggering scheme is best).

8 Summary

This paper presents an algorithm for taking consistent logical checkpoints. The proposed algorithm ensures that physical checkpoints taken by various processes are completely staggered to minimize contention in accessing the stable storage. Experimental results on nCube-2 suggest that the proposed scheme can improve performance as compared to existing staggering techniques, particularly when processes synchronize infrequently and message sizes are not very large. The paper also suggests a few variations of the proposed scheme, including an approach for staggering checkpoints when multiple stable storages are available.

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